

# A sub-grid model for the growth of dust particles in hydrodynamical simulations of protoplanetary disks

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## Outline:

- i. Introduction & hydrodynamical code
- ii. Dust coagulation
- iii. Results
- iv. Summary

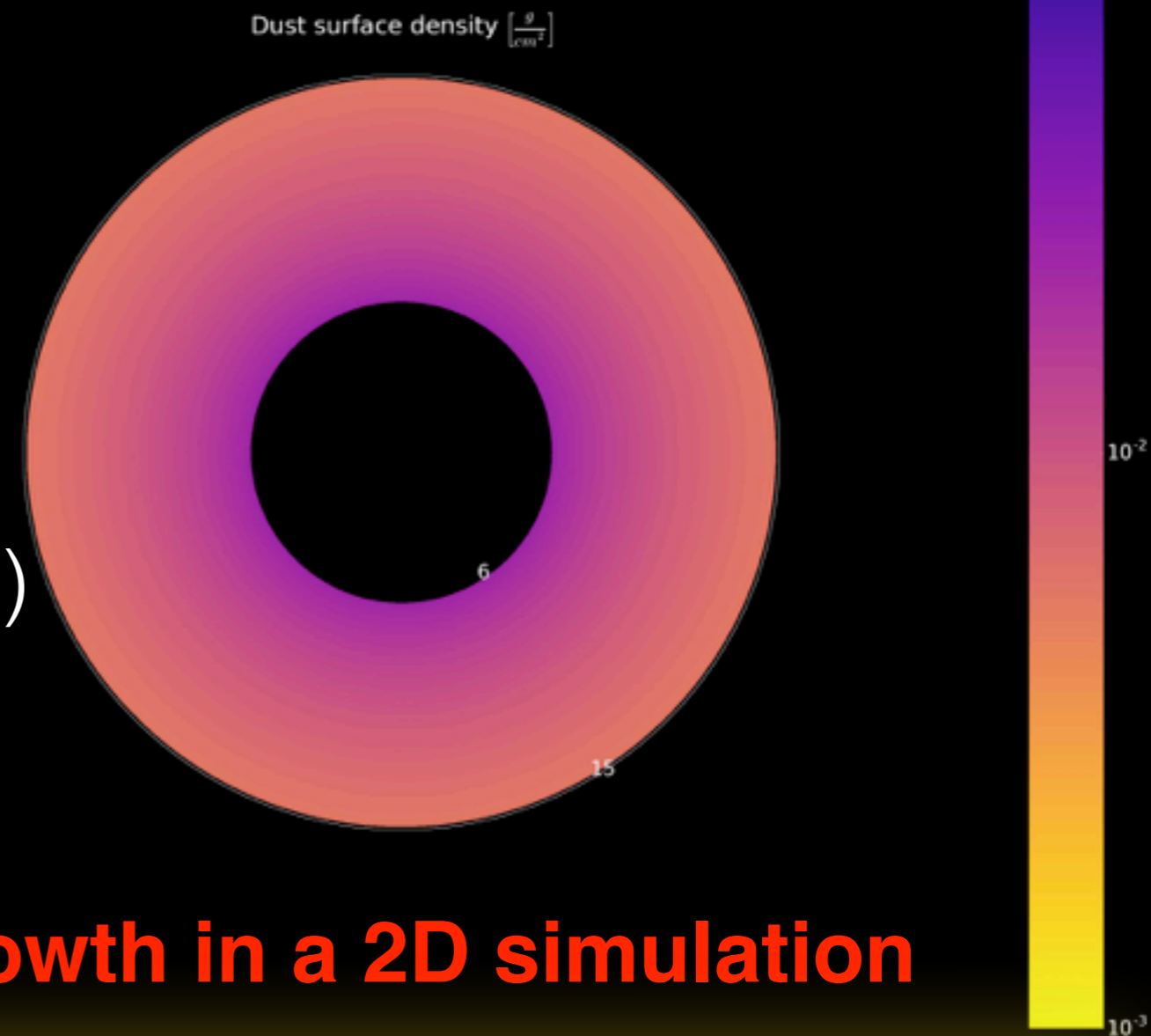
# Introduction & hydrodynamical code

## Current simulations of protoplanetary disks:

- 2D fluid dynamical simulations  
(*e.g. RoSSBi*)
- Fixed dust size  
(i.e. no coagulation)

Goal:

**Implement dust growth in a 2D simulation**



RoSSBi: Explained by Clement Surville



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# Method

Idea: *(based on Birnstiel et al 2012)*

- Determine maximum particle size from full 1D simulations
- Find semi analytical expressions of maximum sizes

$$a_{\max} \propto f(\Sigma_{g,d}, P, \rho_s, \dots)$$

- Compare with full simulations and find coefficients

$$a_{\max} = C_{\text{experimental}} \cdot f(\Sigma_{g,d}, P, \rho_s, \dots)$$

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# What are the maximum values?

✓  $a_{\text{drift}}$ :

Drift limited size

✓  $a_{\text{df}}$ :

Drift induced fragmentation

✓  $a_{\text{frag}}$ :

Turbulence induced fragmentation



✓  $a_{\text{ini}}$ :

Simulation of the initial growth

New size



Maximum size

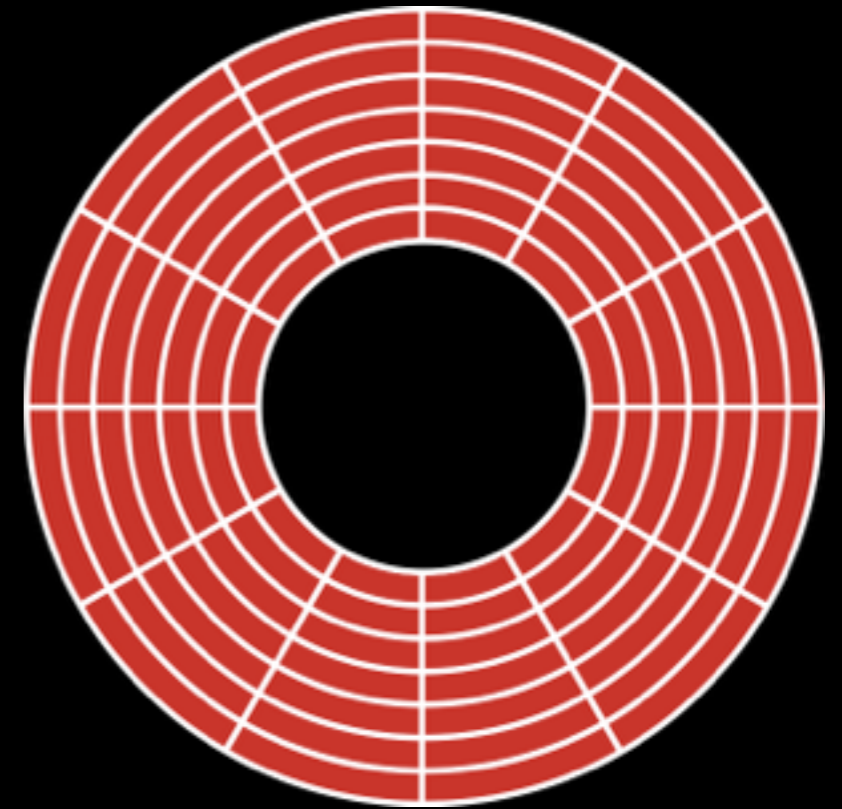


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# Implementation

Algorithm *in RoSSBi*:



- 2D Disk
- Go through each cell and find the maximum size of the particles
- Dust density is governed by maximum size

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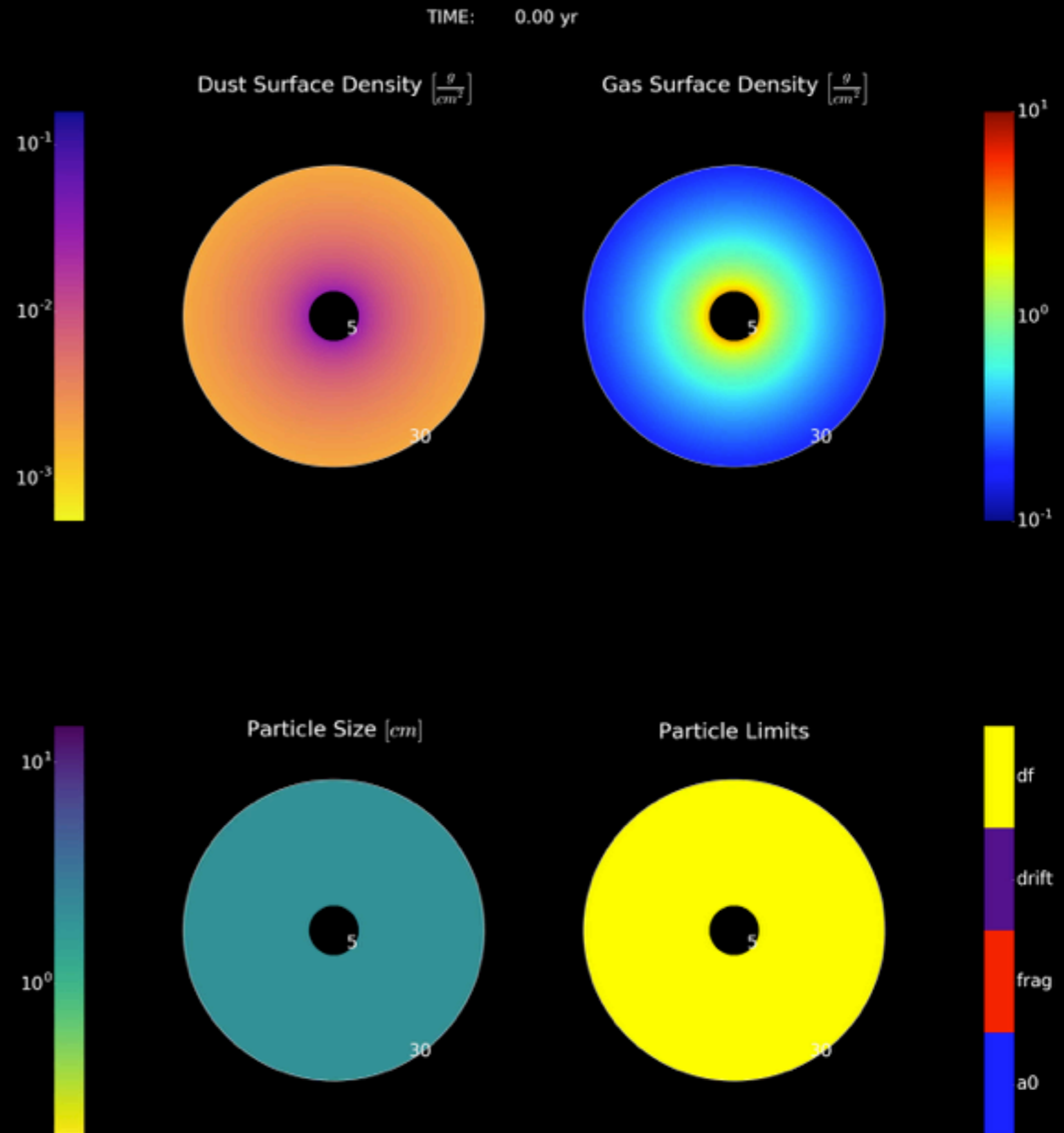
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### Details:

- Planet 1.6 earth mass
- Disk: 5 - 30 AU
- Starting dust size 2 cm
- Dust to gas:  $10^{-2}$
- Gas model:

$$\Sigma_g = 1780 \left( \frac{r}{AU} \right)^{-1} \left[ \frac{g}{cm^2} \right]$$

# Results



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# Comparison (*RoSSBi vs RoSSBi*)

## Comparison: *RoSSBi vs RoSSBi (& growth)*

- Planet: *Jupiter mass*
- Disk: *5 - 30 AU*
- Particle size 1: *3 cm*
- Particle size 2:  *$10^{-4}$  cm*
- Particle size 3:  *$10^{-4}$  cm*
- Dust to gas:  *$10^{-2}$*
- Gas model: *Minimum Mass Solar Nebula*

## Outline:

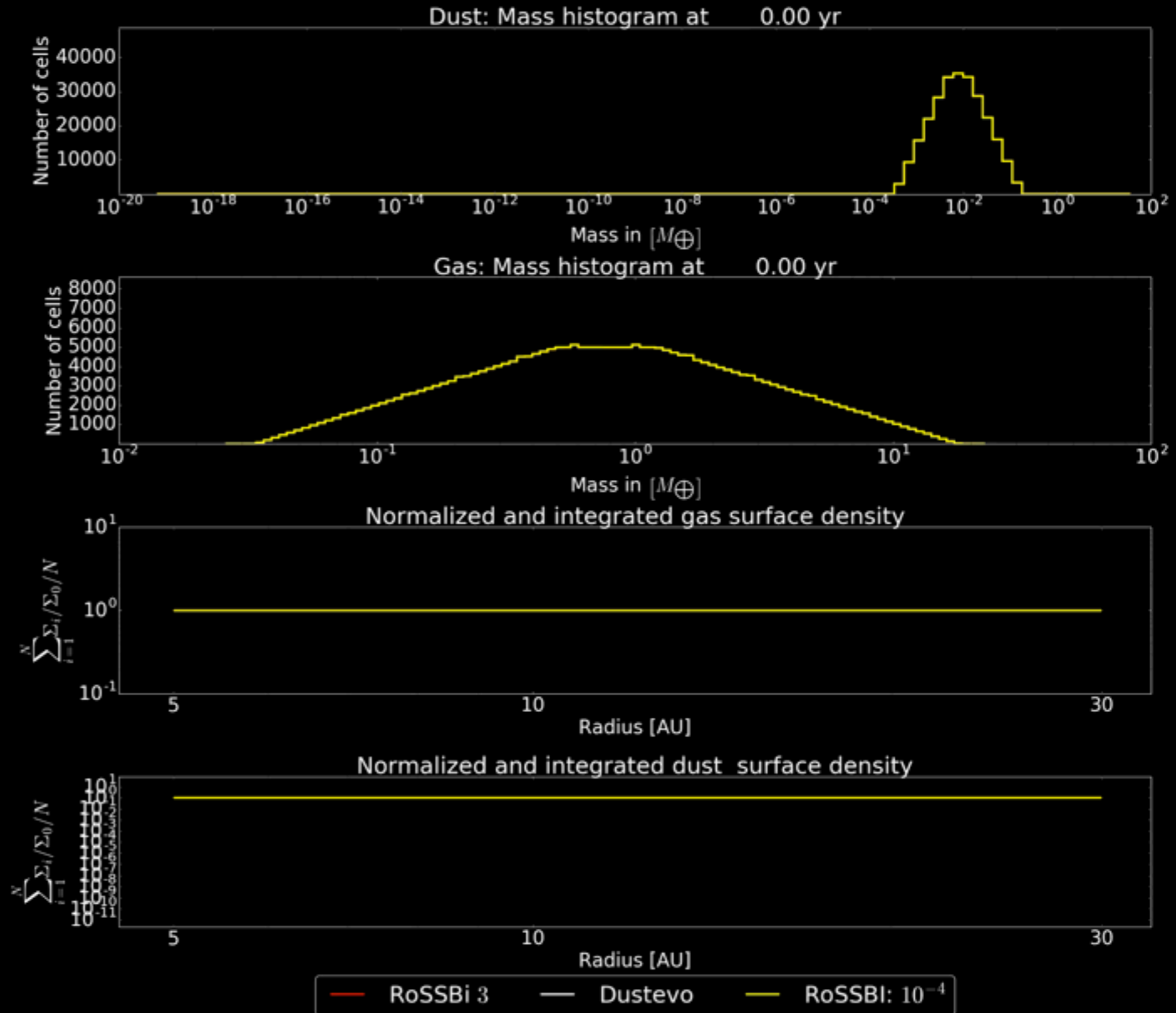
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## Comparison:

- *Jupiter mass*
- *5 - 30 AU*
- *3 cm*
- $10^{-4} \text{ cm}$
- $10^{-4} \text{ cm}$
- $10^{-2}$
- *MMSN*

# Comparison (*RoSSBi vs RoSSBi*)

TIME: 0.00 yr





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# Comparison (*RoSSBi vs cylindrical ATHENA*)

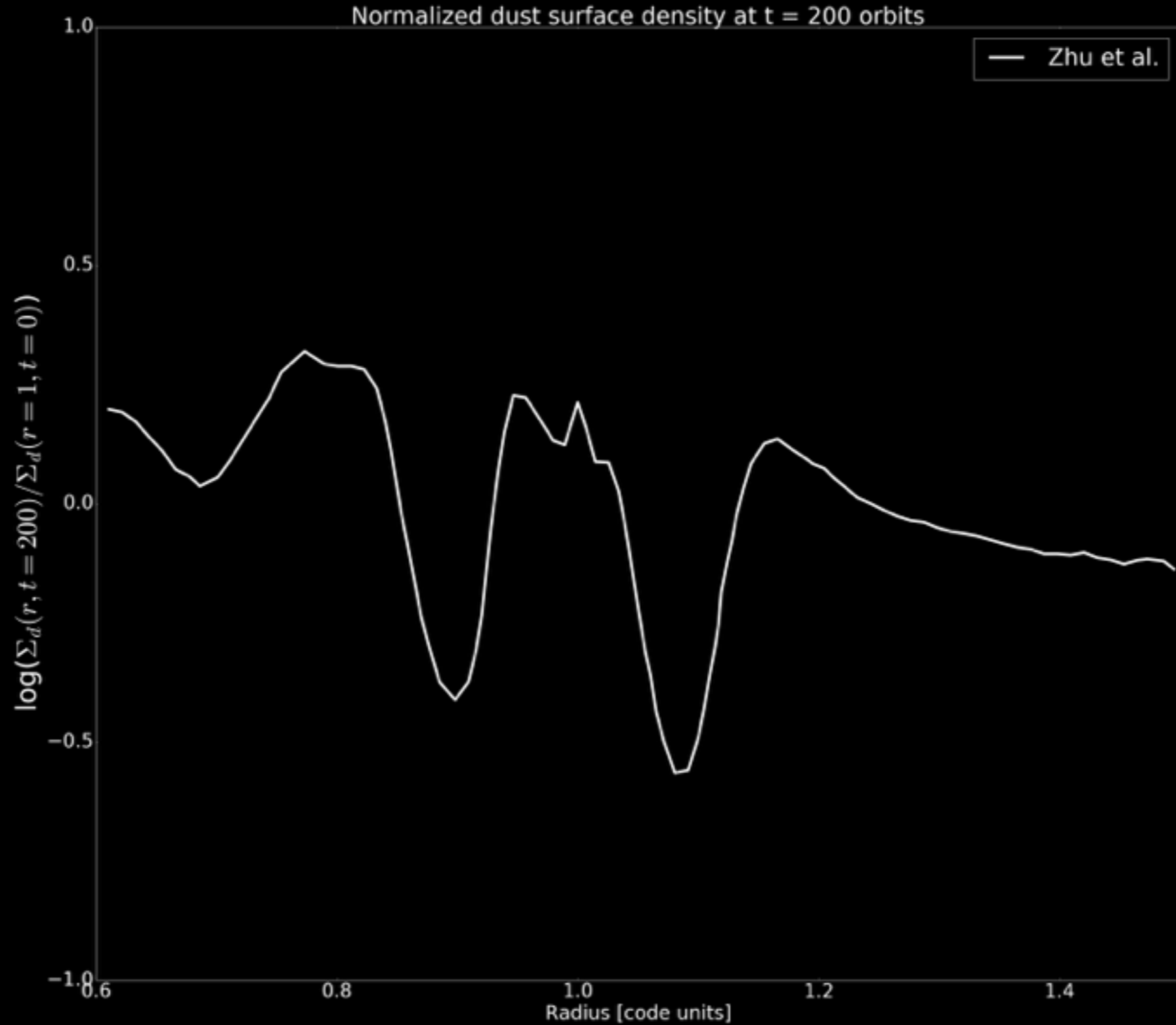
## Comparison: *RoSSBi vs ATHENA* (Zhu et al. 2012)

- Planet: *1.6 earth masses*
- Disk: *0.5 - 3.0 [Code units]*
- Particle size: *2 cm*
- Gas model:  $\Sigma_g = 1780 \left(\frac{r}{AU}\right)^{-1} \left[\frac{g}{cm^2}\right]$
- Evolution time: *200 orbits (~ 6000 yr)*
- Dust to gas:  $10^{-2}$

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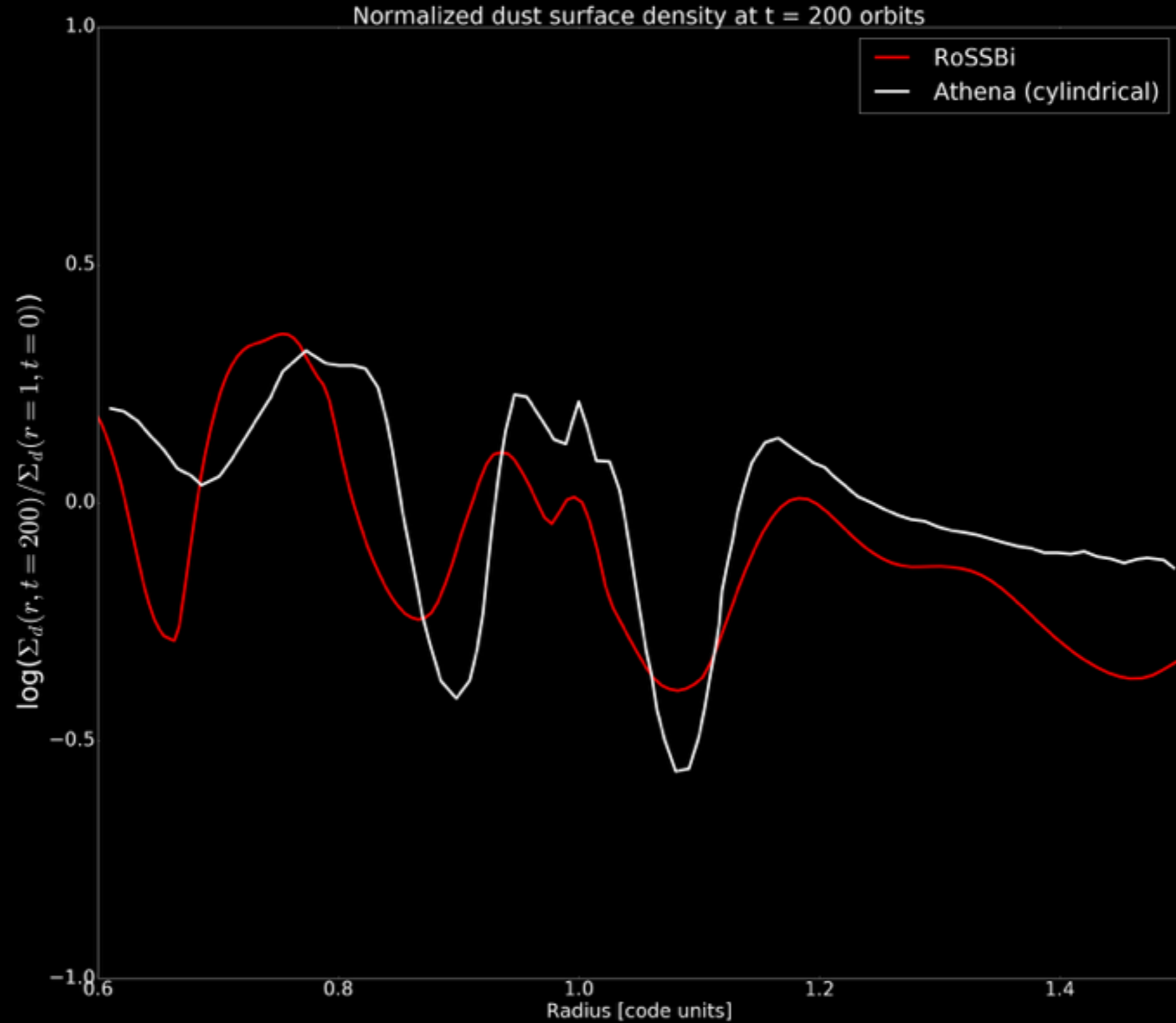
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# Comparison (*RoSSBi vs cylindrical ATHENA*)



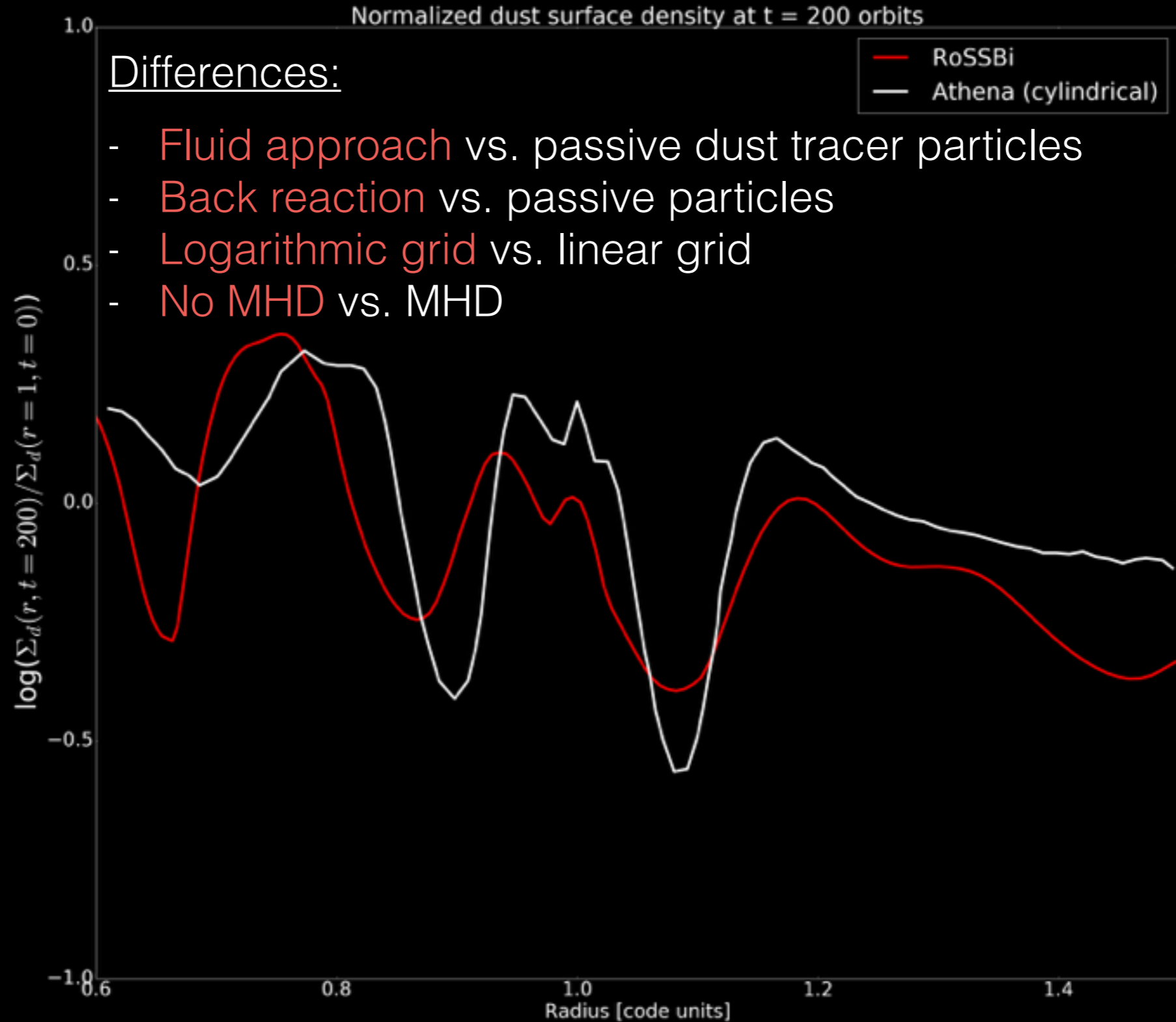
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# Comparison (*RoSSBi vs cylindrical ATHENA*)

## Differences:

- Fluid approach vs. passive dust tracer particles
- Back reaction vs. passive particles
- Logarithmic grid vs. linear grid
- No MHD vs. MHD

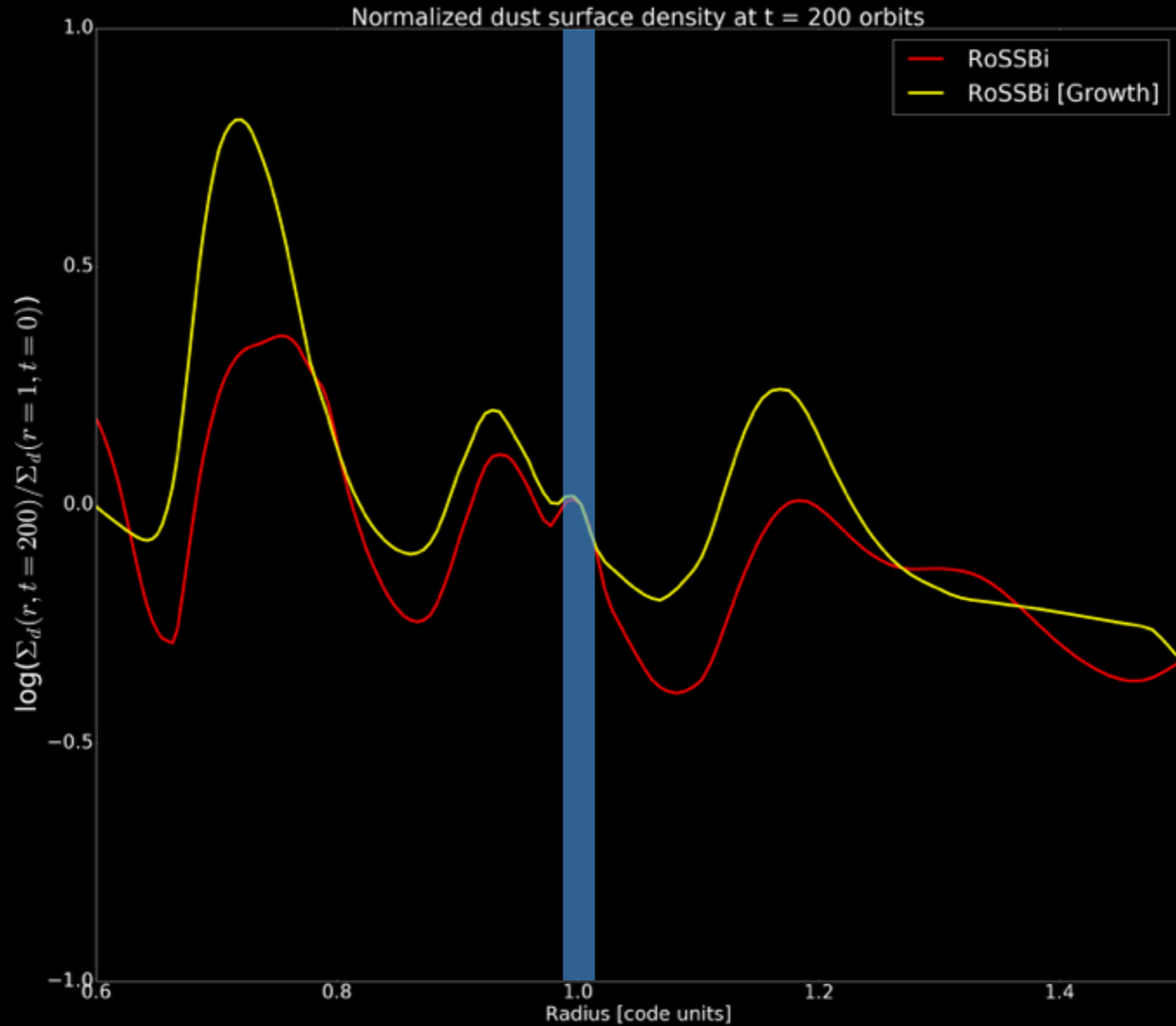




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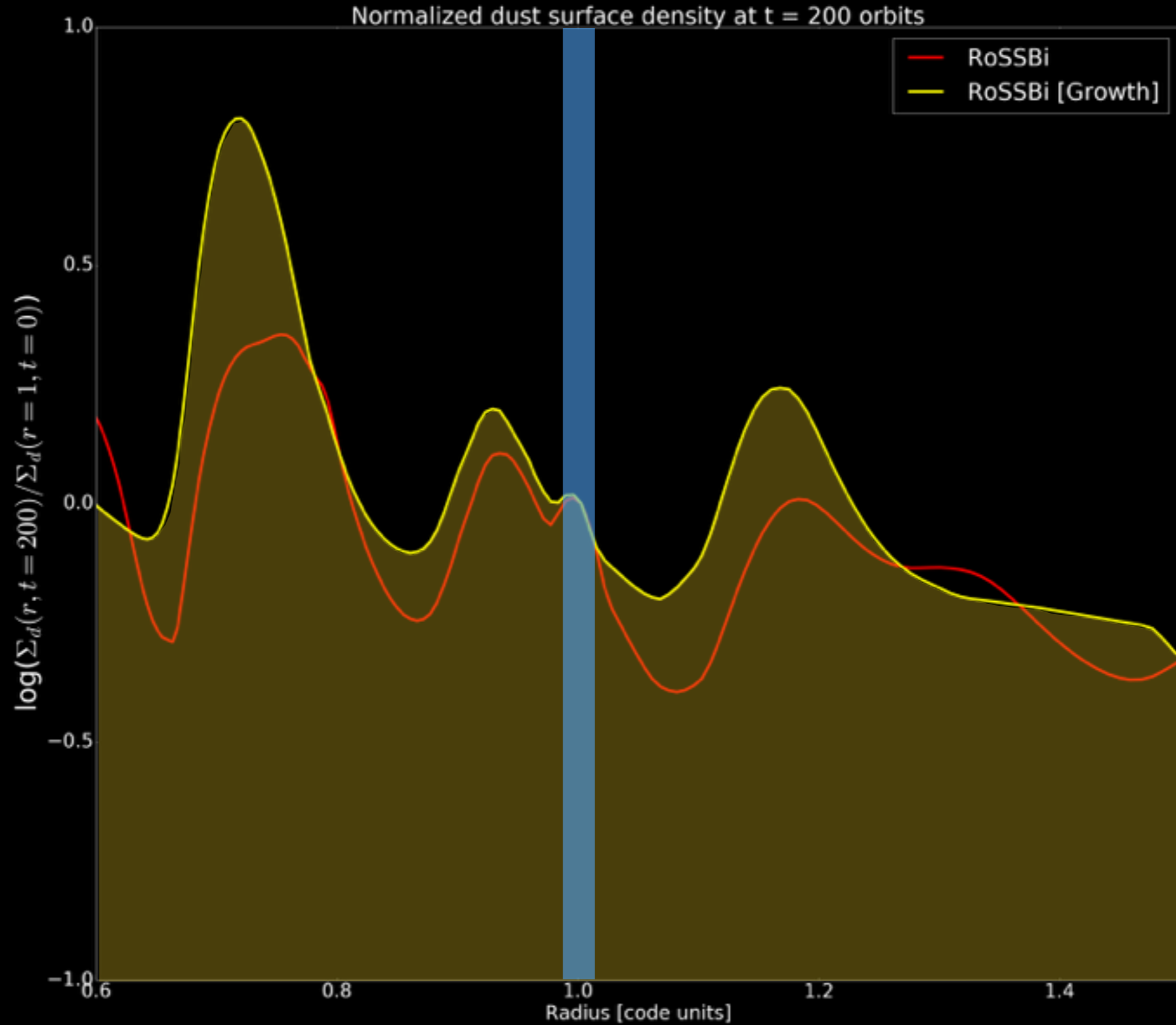
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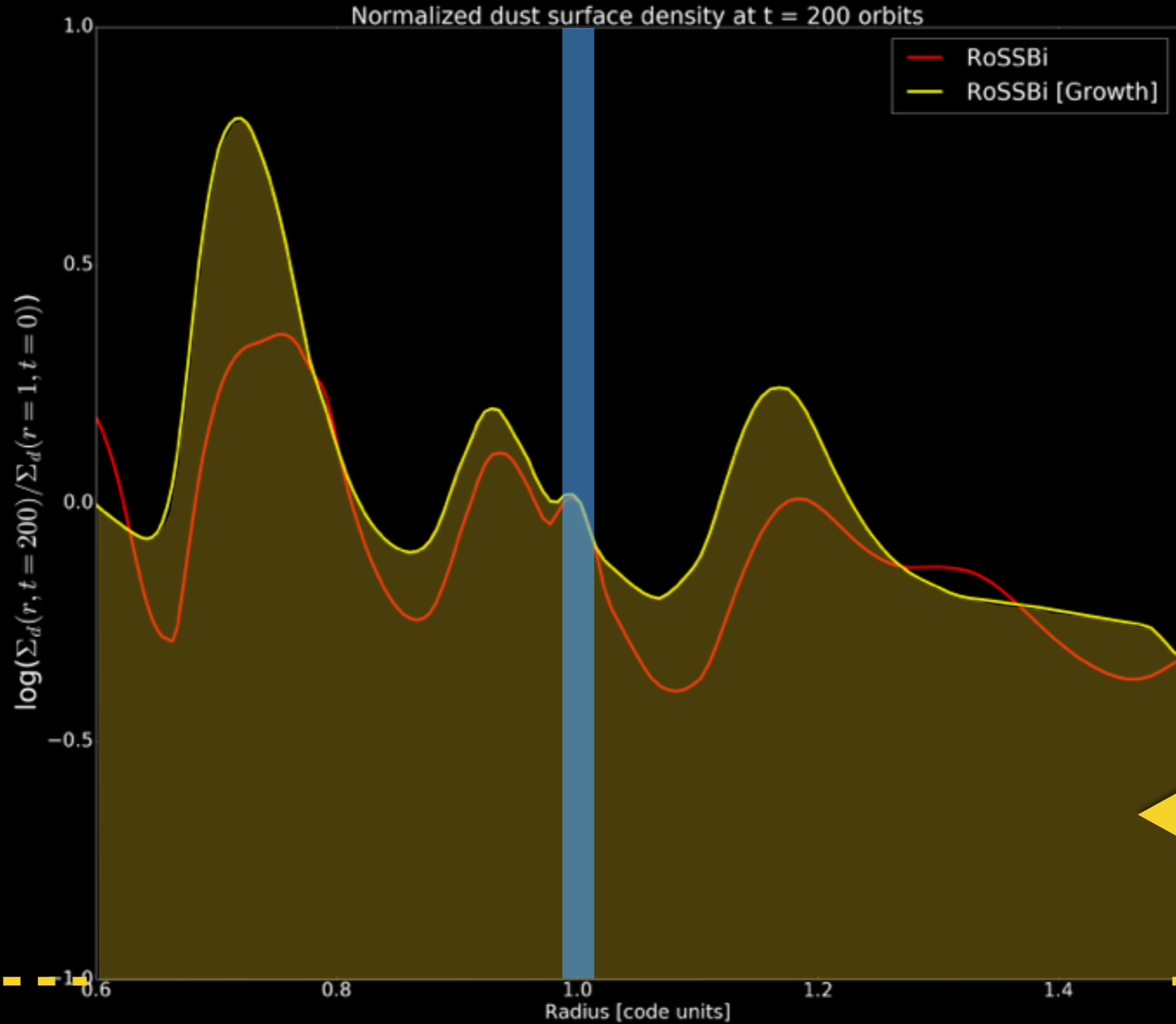
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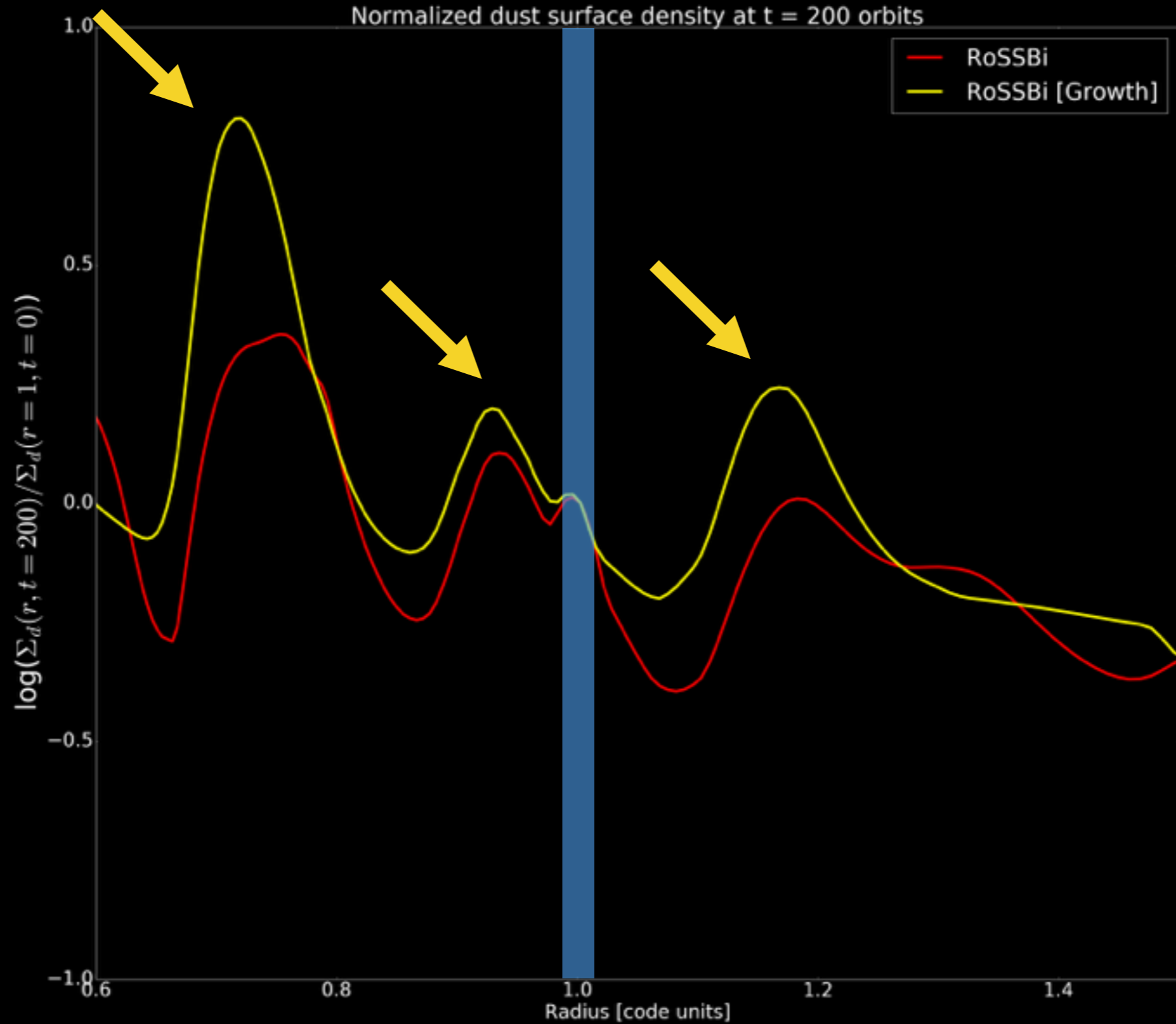
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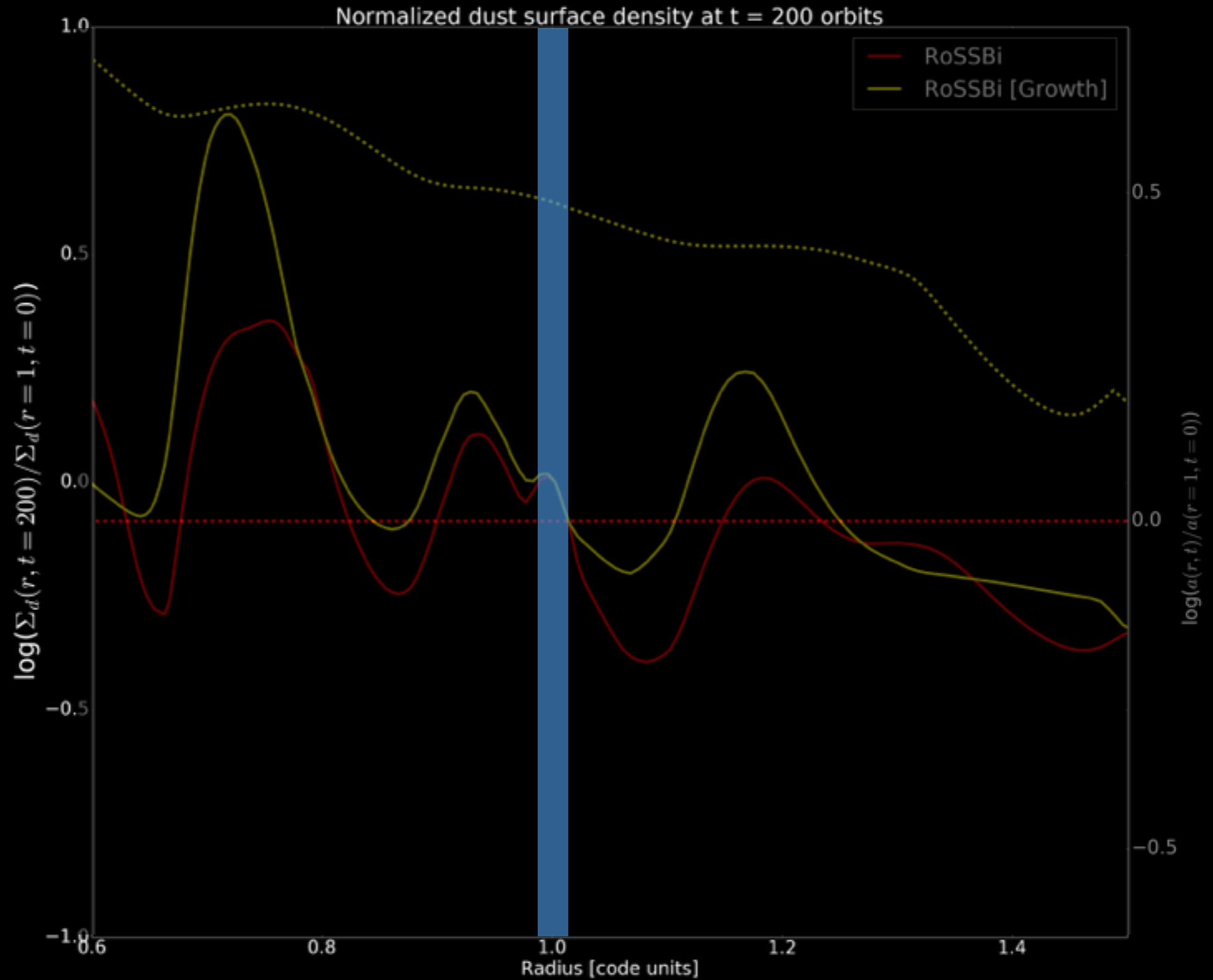




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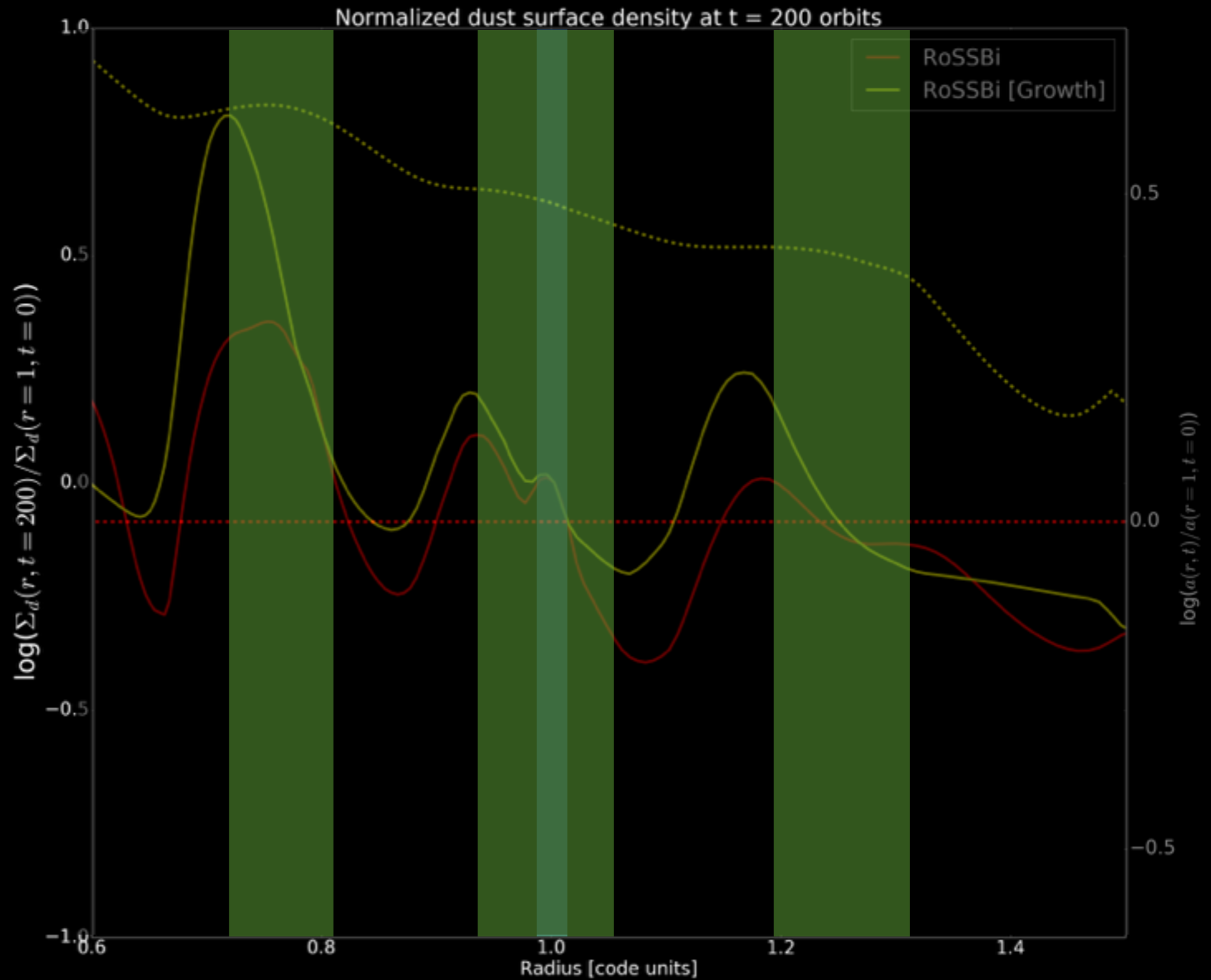
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# Summary

## Take home messages:

- Dust growth is important!
- A variable dust size affects the evolution of protoplanetary disks.
- *For fixed dust simulations: Intermediate dust size.*

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THANK YOU FOR YOUR ATTENTION!